

3.

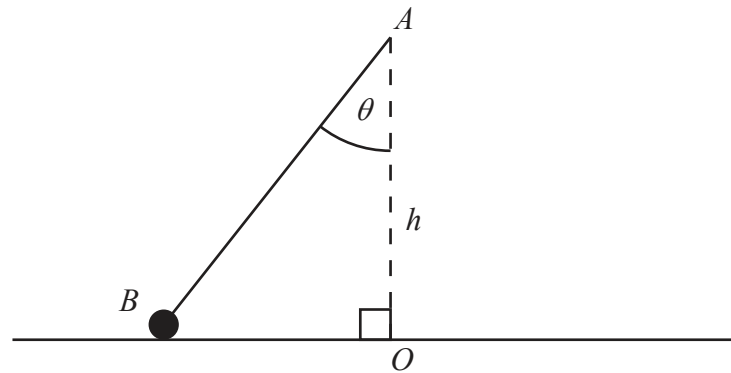


Figure 2

Figure 2 shows a particle B , of mass m , attached to one end of a light elastic string. The other end of the string is attached to a fixed point A , at a distance h vertically above a smooth horizontal table. The particle moves on the table in a horizontal circle with centre O , where O is vertically below A . The string makes a constant angle θ with the downward vertical and B moves with constant angular speed ω about OA .

(a) Show that $\omega^2 \leq \frac{g}{h}$. (8)

The elastic string has natural length h and modulus of elasticity $2mg$.

Given that $\tan\theta = \frac{3}{4}$,

(b) find ω in terms of g and h . (5)



4.

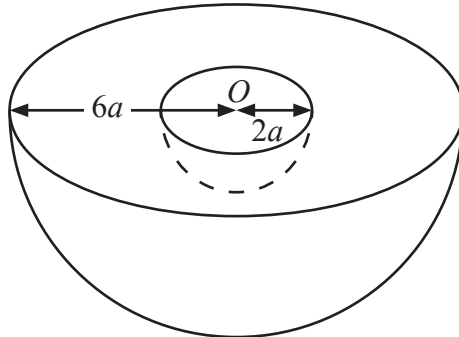


Figure 3

A uniform solid hemisphere, of radius $6a$ and centre O , has a solid hemisphere of radius $2a$, and centre O , removed to form a bowl B as shown in Figure 3.

(a) Show that the centre of mass of B is $\frac{30}{13}a$ from O . (5)

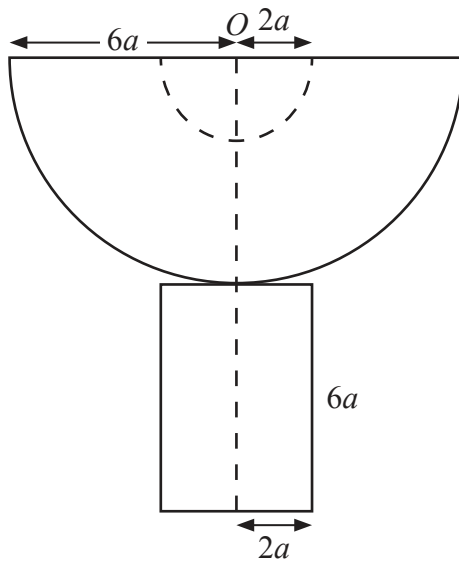


Figure 4

The bowl B is fixed to a plane face of a uniform solid cylinder made from the same material as B . The cylinder has radius $2a$ and height $6a$ and the combined solid S has an axis of symmetry which passes through O , as shown in Figure 4.

(b) Show that the centre of mass of S is $\frac{201}{61}a$ from O . (4)

The plane surface of the cylindrical base of S is placed on a rough plane inclined at 12° to the horizontal. The plane is sufficiently rough to prevent slipping.

(c) Determine whether or not S will topple. (4)



